

# Math 243

Q5 
$$\frac{2x^4 + x^2 - 3}{(x+2)^2(x-3)(x^2+1)} = \frac{A}{x+2} + \frac{B}{(x+2)^2} + \frac{C}{x-3} + \frac{Dx+E}{x^2+1}$$

$$2x^4 + x^2 - 3 = A(x+2)(x-3)(x^2+1) + B(x-3)(x^2+1) + C(x+2)(x^2+1) + (Dx+E)(x+2)(x-3)$$

by textbook lets roots:  $-2, 3, \pm i$       lets  $x = \text{anything}$   $\rightarrow$  eqs for system of eqns

lets  $x=3$        $2(3)^4 + 3^2 - 3 = C(3+2)^2(3^2+1)$

lets  $x=-2$

vs equality of polynomials

$$2x^4 + x^2 - 3 = A(x^4 - x^3 - 5x^2 - x - 6) + B(x^3 - 3x^2 + x - 3) + C(x^4 + 4x^3 + 5x^2 + 4x + 4) + D(x^4 + x^3 - 8x^2 - 12x) + E(x^3 + x^2 - 8x - 12)$$

$x^4$	$A + C + D = 2$
$x^3$	$-A + B + 4C + D + E = 0$
$x^2$	$-5A - 3B + 5C - 8D + E = 1$
$x$	$-A + B + 4C - 12D - 8E = -1$
const	$-6A - 3B + 4C - 12E = 0$

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$$\frac{1}{(x+1)(x-2)(x+3)} = \frac{A}{x+1} + \frac{B}{x-2} + \frac{C}{x+3} \quad \text{roots: } \begin{matrix} -1 \\ 2 \\ -3 \end{matrix}$$

$$1 = A(x-2)(x+3) + B(x+1)(x+3) + C(x+1)(x-2)$$

lets  $x=2$        $B = 1/5$  etc

$$\int \frac{1 + 0 - e^x - e^x}{1 + e^x} dx = \int \frac{(1 + e^x) - (e^x)}{1 + e^x} dx$$

↑  
be creative!

$$\int e^{-x} \cdot \frac{e^x}{1 + e^x} dx$$

$$\int \frac{1 + e^x}{1 + e^x} - \frac{e^x}{1 + e^x} dx$$

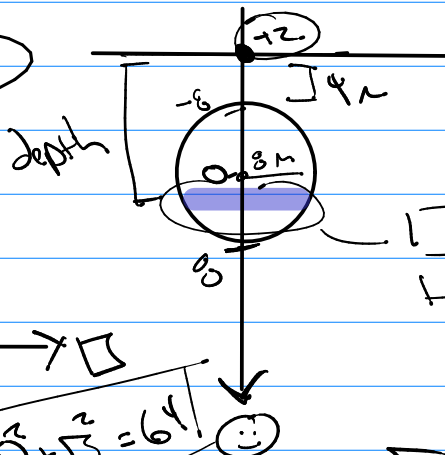
$$\rightarrow \int \left( 1 - \frac{e^x}{1 + e^x} \right) dx$$

$$\int \frac{1}{1 + e^x} dx = \int \frac{1}{u} \frac{du}{u-1} = \int \frac{1}{u(u-1)} du$$

$$u = 1 + e^x \Rightarrow e^x = u - 1$$

$$du = e^x dx \Rightarrow dx = \frac{du}{u-1}$$

8.3 #5



$$F_i = (\delta) (\text{Area}) (\text{depth})$$

$$\int \text{Area} \, d(\odot)$$

$$\text{width} = 2\sqrt{64 - (\odot)^2}$$

$$F_i = (\delta) (2\sqrt{64 - (\odot)^2}) (\odot + 12)$$

$$2\delta \int_0^8 \sqrt{64 - (\odot)^2} (\odot + 12) d(\odot)$$

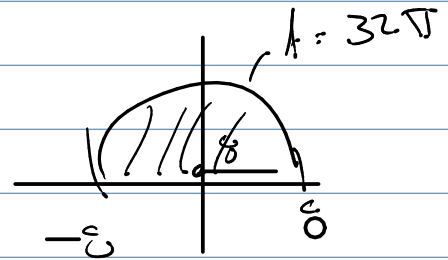
$$28 \int_{-8}^8 \sqrt{64 - x^2} (x + 12) dx$$

$$= 28 \left[ \int_{-8}^8 x \sqrt{64 - x^2} dx + 12 \int_{-8}^8 \sqrt{64 - x^2} dx \right]$$

$$\text{let } u = 64 - x^2$$

$$du = -2x dx$$

$$= 28 \left[ -\frac{1}{2} \int_0^0 u^{1/2} du \right]$$



Ch 9

## Differential Equations

① eq 5 see " $\Rightarrow$ " expression = expression

↑  
can now include  $\frac{d}{dx}[f]$

$$\text{ex } \frac{dT}{dt} = -3T$$

② Soln  $\rightarrow$  find an equation for a function such that it make the diff eqn true.

②  $\frac{df}{dt} = k \cdot f \rightarrow f(t) = \text{expression}$

↑  
find?

→ Lösung: Separabel:

$$T = ?$$

$$\frac{dT}{dt} = -3T$$

$$\frac{1}{T} dT = -3 dt$$

$$\int \frac{1}{T} dT = \int -3 dt$$

$$\ln T = -3t + C$$

$$T = e^{-3t + C}$$

$$T = e^{-3t} \cdot e^C = C$$

$$T = C e^{-3t}$$

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