

Math 451

~~Q's/~~ ① Project 5

② Exam

Derivative (c)

Derivative (f, a)

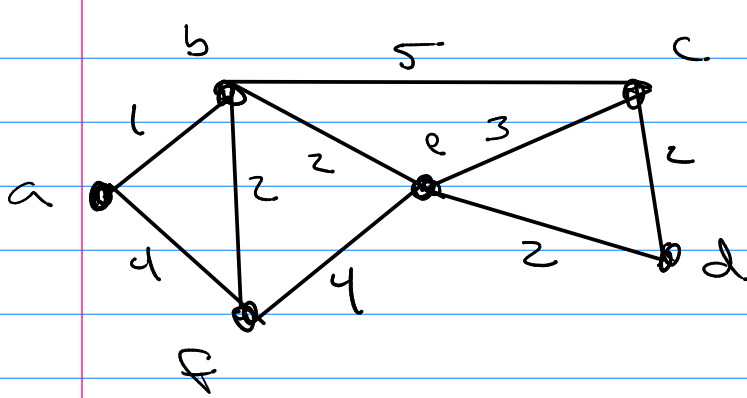
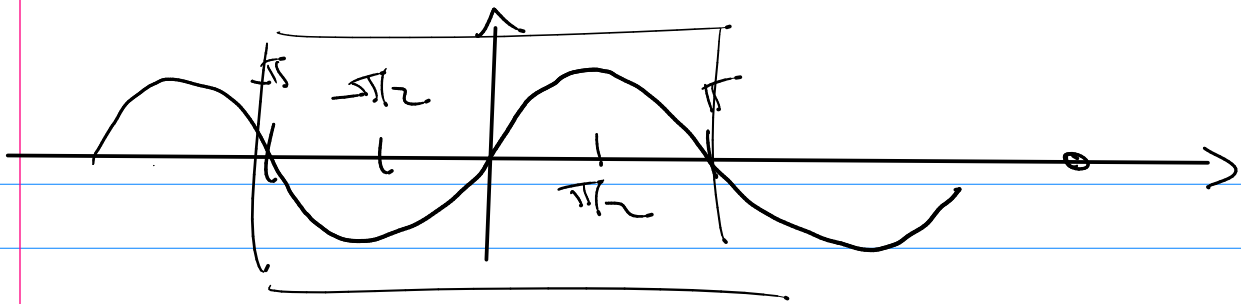
ex: $f(x) = 3x^2 + 2x - 7$ $f'(x) = 6x + 2$
 $[3 \ 2 \ -7]$ $[6 \ 2]$

ex: $f(x) = 3x^2 + 2x - 7$ $a = 1$
 $f'(1) = 8$

Derivative ($[3 \ 2 \ -7]$)
ans = $[6 \ 2]$

→ Derivative ($(a(x) \ 3, *x, 1, 2 + 2, *x - 7, 1)$)
ans = 8

$$f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$$

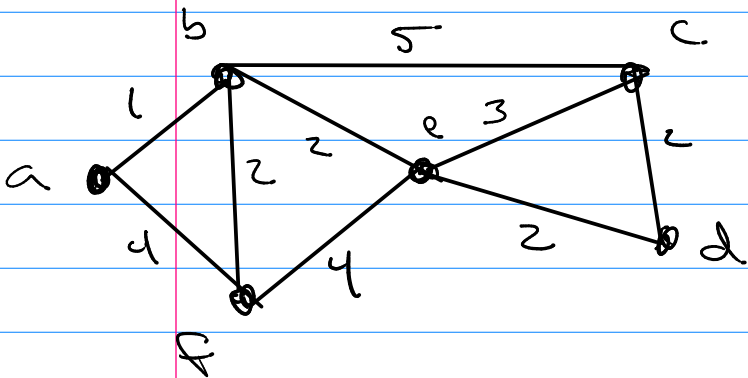


least cost paths from

	Path	Cost
a to a	a	0
b	a,b	1
c	a,b,c	6
d	a,b,e,d	5
e	a,b,e	3
f	a,b,f	3

Dijkstra's Algorithm

G with vertices v_1, v_2, \dots, v_n weights $w(v_i, v_j)$



$$A_G = \begin{matrix} & \begin{matrix} a & b & c & d & e & f \end{matrix} \\ \begin{matrix} a \\ b \\ c \\ d \\ e \\ f \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 4 \\ 1 & 0 & 5 & 0 & 2 & 2 \\ 0 & 5 & 0 & 2 & 3 & 0 \\ 0 & 0 & 2 & 0 & 2 & 0 \\ 0 & 2 & 3 & 2 & 0 & 4 \\ 4 & 2 & 0 & 0 & 4 & 0 \end{bmatrix} \end{matrix}$$

Basics: in A_G make all zeros to ∞
 costs from a to any of the others starts at ∞

for your start vertex: a
Cell array (Path for a is {a})
 (Cost for a is 0)

Pseudocode

process Dijkstra (A_G, a)

for i from 1 to n ← number of vertices

costs of each $v_i = \infty$

cost of $a = 0$

path of $a = \{a\}$

found vertices = $\{a\}$

while not found vertices $\neq \emptyset$

find vertex u not found and cost of

path from a found vertex to u is min

found vertices = $\{ \text{found vertices}, u \}$

cost of $u = \{ \text{path of found} + \text{cost to } u \}$

end

$V = \{a, b, c, d, e\} \rightarrow [1 \ 1 \ 1 \ 1 \ 1]$

have $S = \{a, c, d\} \rightarrow [1 \ 0 \ 1 \ 1 \ 0]$