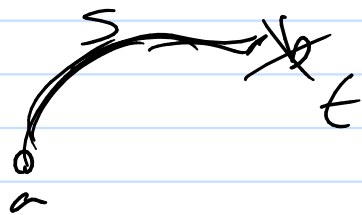


# Math 344

HW? → Mark says: "S or so pebs"

length: ①  $s = \int_a^b |r'| dt$



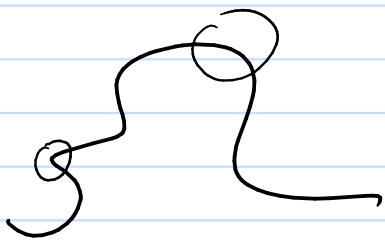
②  $s(t) = \int_a^t |r'(u)| du$

or Fund. th<sup>m</sup>

$$\frac{d}{dt} [s(t)] = |r'(t)|$$

③ if you have  $s = s(t)$  solve for  $t = t(s)$

$$\text{so } \underline{r(t)} = r(t(s)) = \underline{r(s)}$$



$\mathcal{B} \propto d\pi$

$\mathcal{B} \propto \frac{1}{ds}$

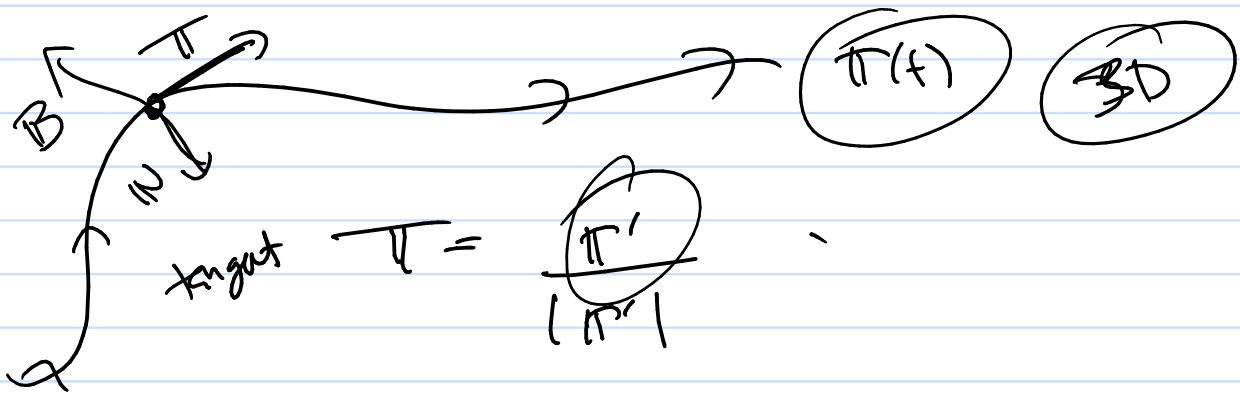
Curvature  $\mathcal{K} = \left| \frac{d\pi}{ds} \right|$

$\pi = \frac{\pi'(t)}{|\pi'(t)|}$

$$\mathcal{K}(t) = \left| \frac{\frac{d\pi}{dt}}{\frac{ds}{dt}} \right| = \frac{|\pi'|}{|\dot{r}|}$$

Note:  $\pi = \angle(x, y, z)$

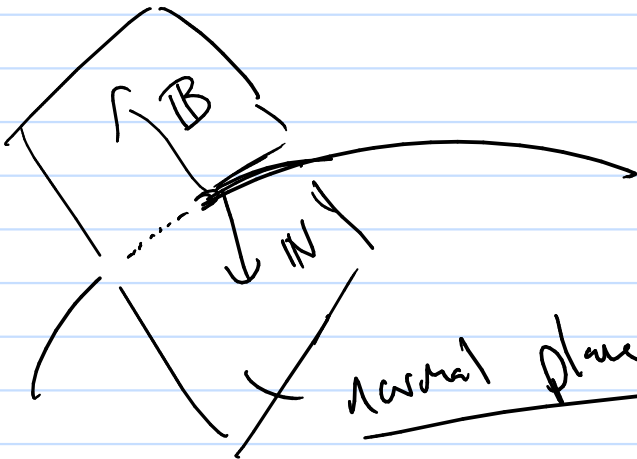
$$\mathcal{K} = \frac{|\pi'|}{|\dot{r}|} = \frac{|\dot{r}' \times \dot{r}''|}{|\dot{r}'|^3}$$



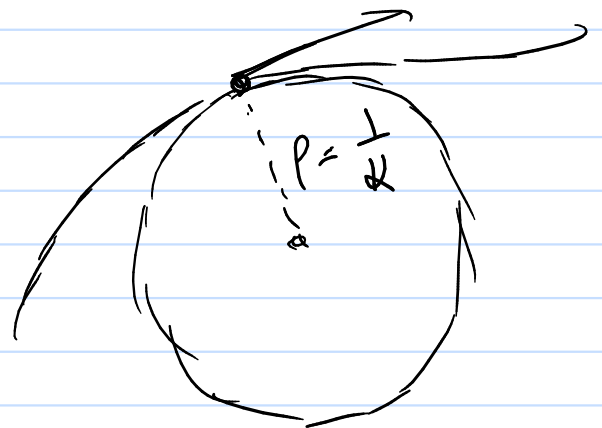
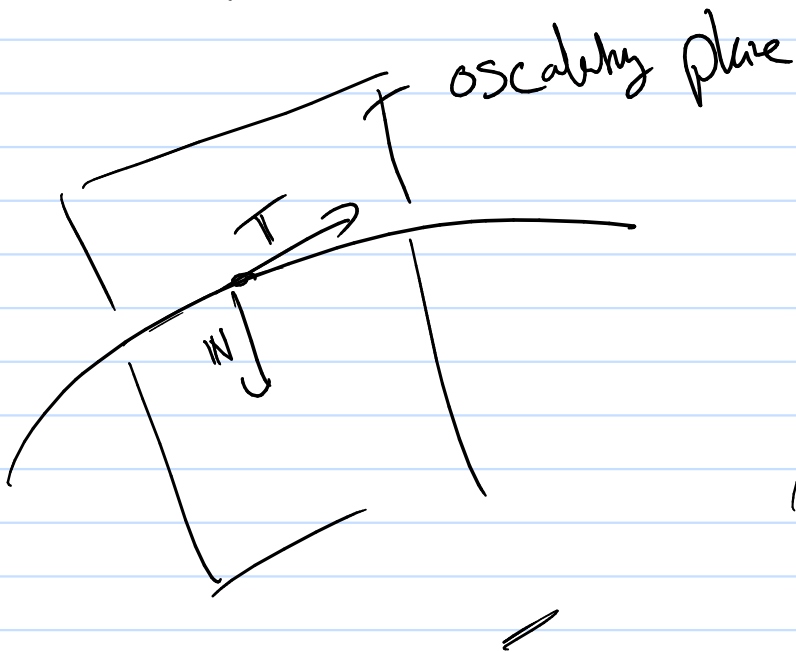
Tangent  $T = \frac{\pi'}{|\pi'|}$

Normal  $N = \frac{\pi''}{|\pi''|}$

binormal  $B = T \times N$



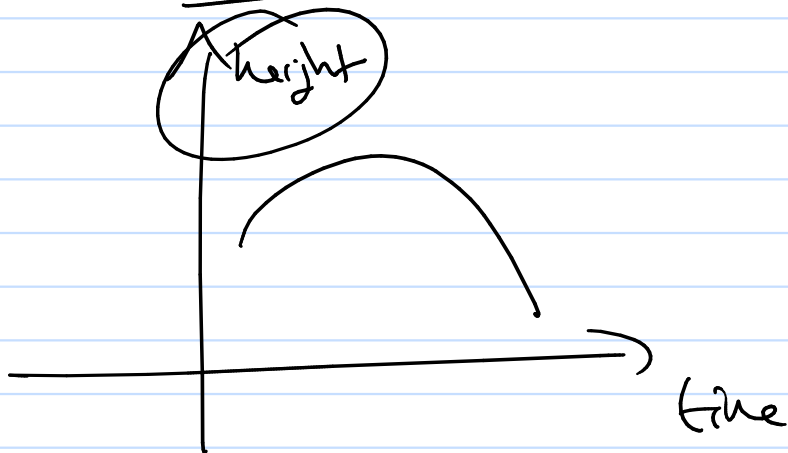
normal plane is  $\perp$  to Tangent



13.4

# Motion in Space

Calc



$$\text{position} = s(t)$$

$$\text{vel} = v(t) = s'(t)$$

$$\text{accel} = a(t) = v'(t) = s''(t)$$

$$\text{Force} = \text{change in momentum} = \frac{d}{dt} [\text{mass} \cdot \text{vel}]$$

$$F = ma$$

$$\begin{aligned} a &= a(t) \\ \int & \\ v &= \int a(t) dt \\ \int & \\ r &= \int v(t) dt \end{aligned}$$



Monday: Review

Wed:

24 open for exam.

Friday:

"grade Exam 1"