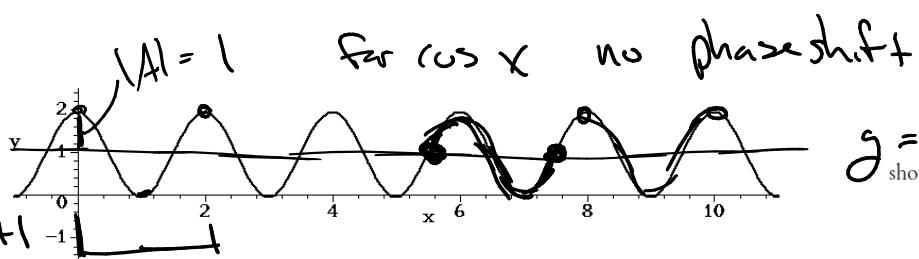


Math 112

C's

The figure



$g = 1$ shows the graph of the

$$y = 1 + \cos(\pi x + \phi) + 1$$

function

$$f(x) = \cos(\pi x) + 1$$

$$\text{Period} = 2 = \frac{2\pi}{\omega} \quad \text{So} \quad \omega = \pi$$

$$A \cos(\omega x + \phi) + B$$

freq — phase

$$A \sin(\omega x + \phi) + B$$

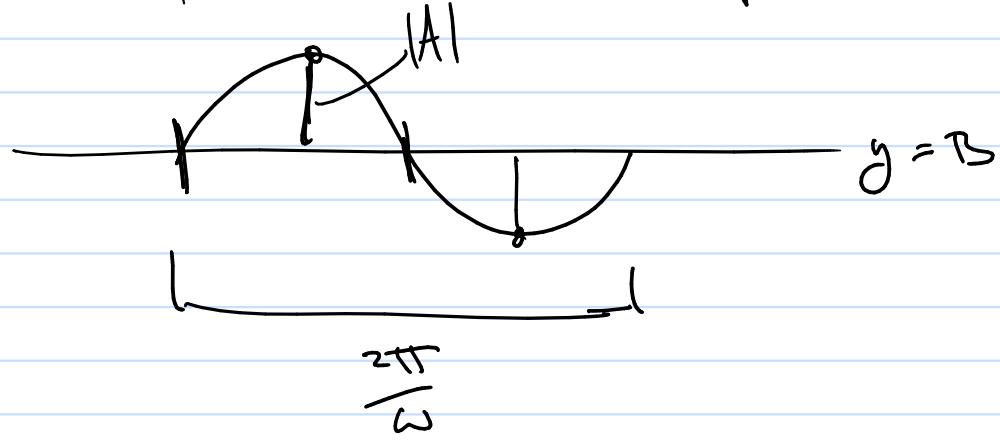
$$\text{amplitude} = |A|$$

$$\text{phase shift} = -\frac{\phi}{\omega}$$

$$\text{Period} = \frac{2\pi}{\omega}$$

$$\text{vertical shift} = B$$

$$1 \longleftrightarrow 1 \quad \text{horz. shift} = \text{phase shift} = -\frac{\phi}{\omega}$$



$$f(t) = A \cos(\omega t + \phi) + B$$

$$\cos(\alpha t + \phi)$$

6

Suppose $y = -4 \cos(9t + 6) + 3$. In your answers, enter π for π .

What is the phase shift?

$$\cos\left(\alpha\left(t - \frac{\phi}{\alpha}\right)\right)$$

$$\text{Amplitude} = |A| = 4$$

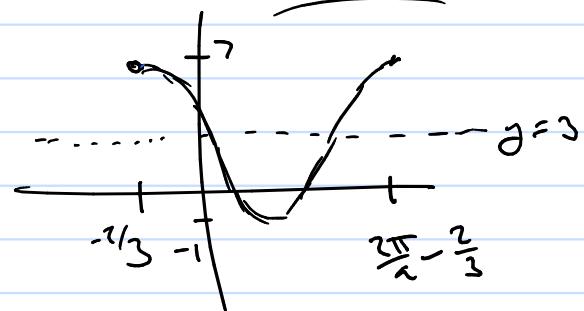
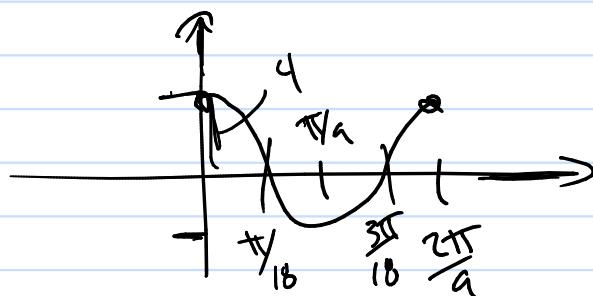
$$\text{phase} = \phi$$

$$\text{freq} = \omega = 9$$

$$\text{phase shift} = -\frac{\phi}{\omega} = -\frac{6}{9} = -\frac{2}{3}$$

$$\text{period} = \frac{2\pi}{\omega} = \frac{2\pi}{9}$$

$$\text{Vertical shift} = 3$$



$$\sec x = \frac{1}{\cos x}$$

$$\csc x = \frac{1}{\sin x}$$

Domain: $x \neq \frac{\pi}{2} + n\pi$
 $n \in \mathbb{Z}$

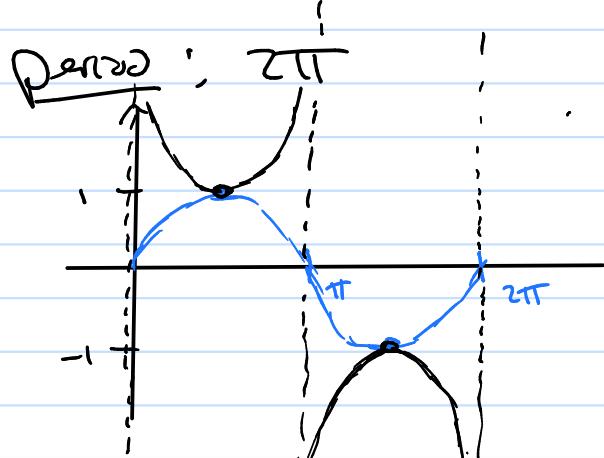
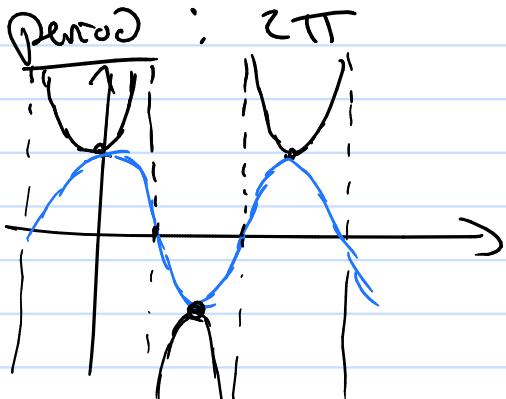
(vertical asymptotes)

Domain: $x \neq 0 + n\pi$

$x \neq n\pi$
 (vertical asymptotes)

Range: $(-\infty, -1] \cup [1, \infty)$

Range: $(-\infty, -1] \cup [1, \infty)$



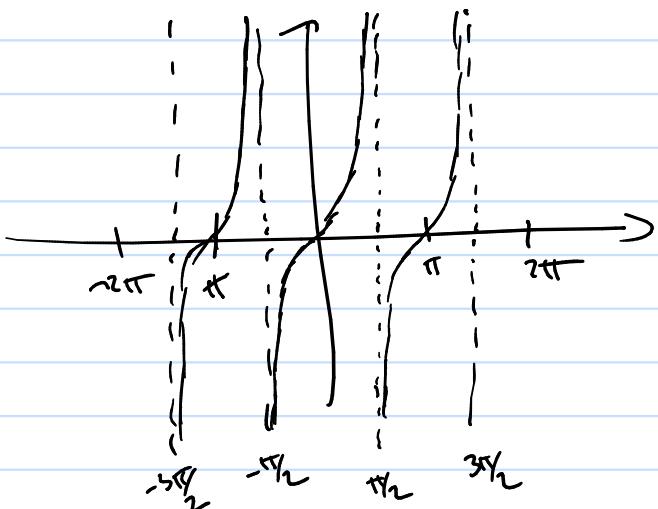
$$\tan x = \frac{\sin x}{\cos x}$$

Domain: $x \neq \frac{\pi}{2} + n\pi$

vert. asym.

Range: $(-\infty, \infty)$

Period: π



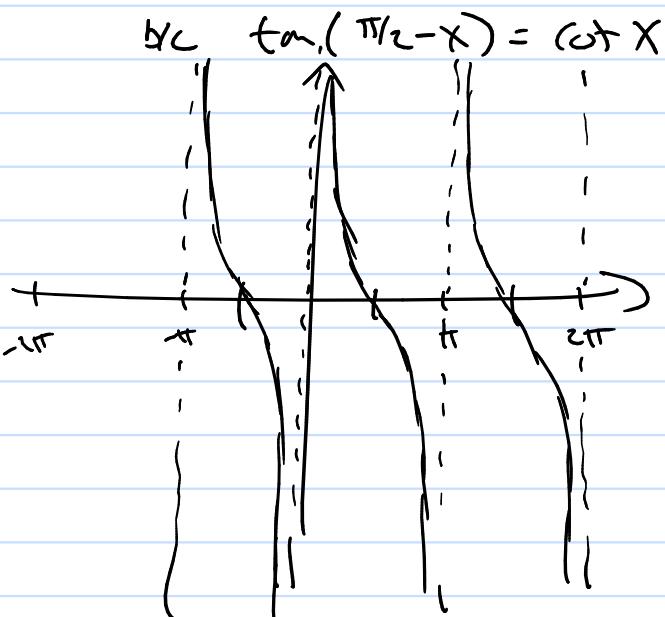
$$\cot x = \frac{\cos x}{\sin x}$$

Domain: $x \neq n\pi$

vertical asym.

Range: $(-\infty, \infty)$

Period: π



What should we all "know" now?!

-
- ① tables for angles and $\cos \theta, \sin \theta$
 - ② All identities
 - ③ Unit Circle w/ $\sin \theta, \cos \theta, \tan \theta, \cot \theta, \sec \theta, \csc \theta$
 - ④ Graphs